

Uncertainties beyond 10-100TeV of Gamma ray & CR phenomena :

「QG effects
on the detection method etc.」

by T. Kifune

10—100 TeV 以上の
ガンマ線には
通常・従来の検出方法を
適用できない

The usual / conventional method of
detecting gamma rays can not be
applied to gamma rays
beyond 10 -100 Tev .

Some comments

- **Relative Delay time = $-5.5 \pm 10.9 \pm 10.3$ [sec TeV⁻¹]**

HESS Beijing 2011, Bolmont et al.

PKS 2155-304, $z=0.116$, $d = 1.4 \times 10^9$ [ly] = 4.2×10^{16} [light sec]

$$M > 2.1 \times 10^{27} \text{ eV} = 0.6 M_{\text{planck}}$$

$$M \approx M_{\text{PL}} = \sqrt{\frac{hc}{2\pi G}} = 1.2 \times 10^{28} [\text{eV} / c^2]$$

- **Modified p-E relation**

$$P^2 c^2 = E^2 - m^2 c^4 + \xi \frac{E^3}{M c^2}$$

$$v = \frac{dE}{dP} = c \left(1 - \frac{E}{M c^2} \right) = c \left(1 - \frac{E}{1 \text{ TeV}} \cdot 10^{-16} \right)$$

- **Systematic errors**

emission time within (1-10) second

Emission size within 10^{10-11} cm

Some comments

- **Relative Delay time = $-5.5 \pm 10.9 \pm 10.3$ [sec TeV⁻¹]**

HESS Beijing 2011, Bolmont et al.

OPERA Oscillation Project with Emulsion-tRacking Apparatus, CERN CNGS1

$$d = 7.3 \times 10^7 \text{ cm} = 2.4 \times 10^{-3} \text{ sec}$$

- **Delay time = $60.7 \pm 6.9 \pm 7.4$ [nsec]**

$$(v - c) / c = (2.4 \pm 0.28 \pm 0.30) \times 10^{-5}$$

MI C

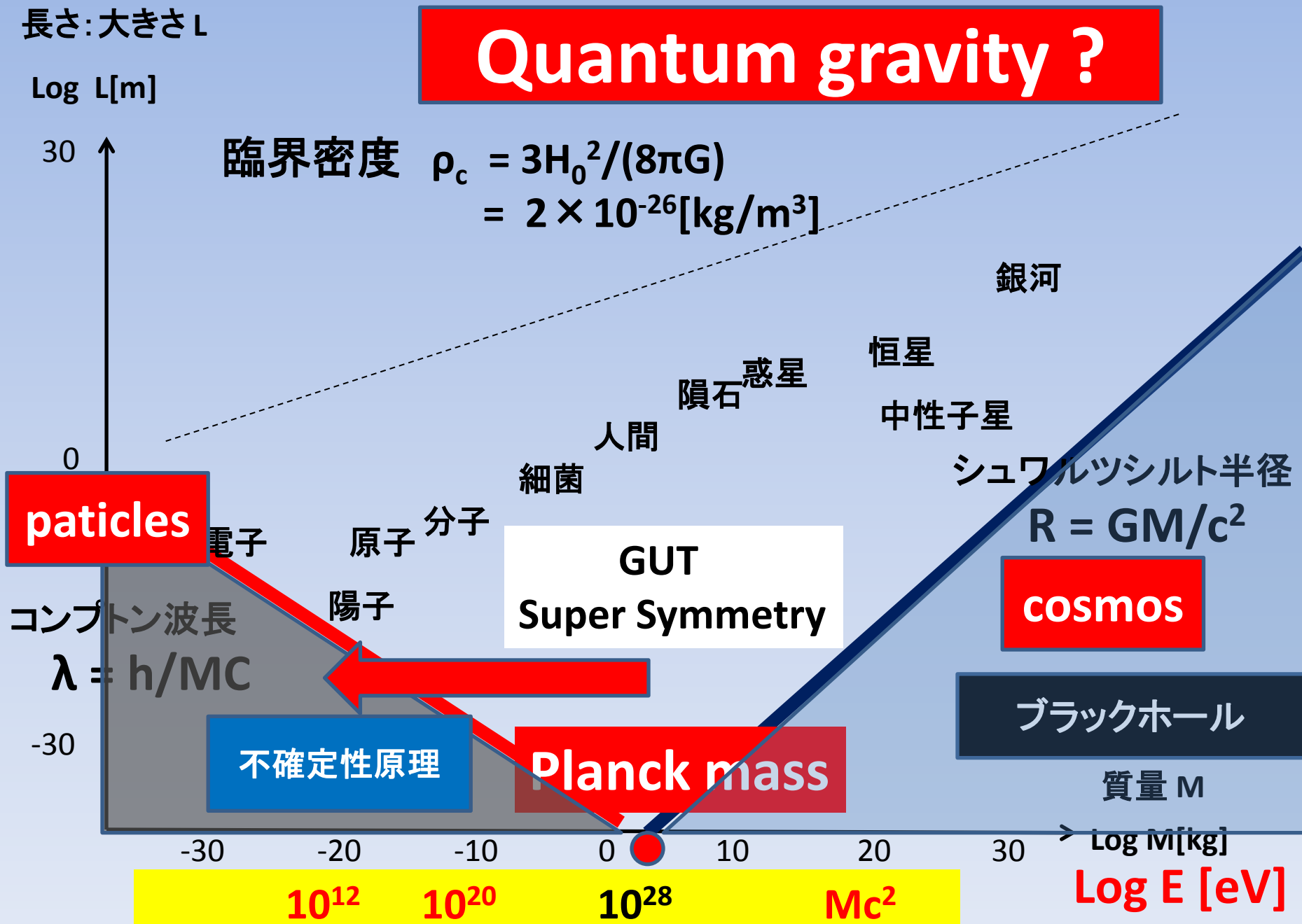
相対論(量子重力理論)の高精度検証

emission time within (1-10) second

Emission size within 10^{10-11} cm

宇宙の構成物の大きさ・質量・密度

Quantum gravity ?



Effect on propagation speed :

- **systematic error ??**
- **higher gamma ray energy**



Effects on astrophysical reactions :

yes /no type test/observation

**Quantum Gravity effect on
VHE gamma ray astrophysics**

- 1. Propagation**
- 2. Emission**
- 3. Detection**

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^+ + e^-$$

absorption

$$e + \varepsilon (\text{EBL}) \rightarrow e + \gamma$$

Inverse
Compton

Interaction with atmosphere

$$\gamma + A \rightarrow e^+ + e^- + A$$

A : atmospheric
nucleus

$$e + A \rightarrow e + \gamma + A$$

Cascade,
Air shower
process

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^+ + e^-$$

Absorption
Pair creation

$$\begin{aligned} k_0 - \varepsilon &\rightarrow p_+ + p_- \\ K_0 + \varepsilon &\rightarrow E_+ + E_- \end{aligned}$$

$\varepsilon \neq 0$ for the process to proceed

Momentum / energy conservation

Effect of

Energy / momentum
of EBL photon

?? term of $\xi K^2 / M_{\text{planck}}$??

$\gamma + \varepsilon \text{ (EBL)} \rightarrow e^+ + e^- \text{ (absorption)}$

$\varepsilon \neq 0$ for the process to proceed

Energy : $K_0 + \varepsilon = E_1 + E_2$

momentum : $\vec{k}_0 - \vec{\varepsilon} = \vec{p}_1 + \vec{p}_2$

Relativistic approximation

QG modification

$$k_0 - \varepsilon = K_0 (1 + \xi K/M)^{0.5} - \varepsilon$$

$$p_1 = E_1 (1 - m_e^2/E_1^2 + \xi E_1/M)^{0.5}$$

$$p_2 = E_2 (1 - m_e^2/E_2^2 + \xi E_2/M)^{0.5}$$

Threshold energy, phase volume,

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^+ + e^-$$

Perpendicular
component

$$K_0 - \varepsilon + \xi K_0^2 / (2M)$$

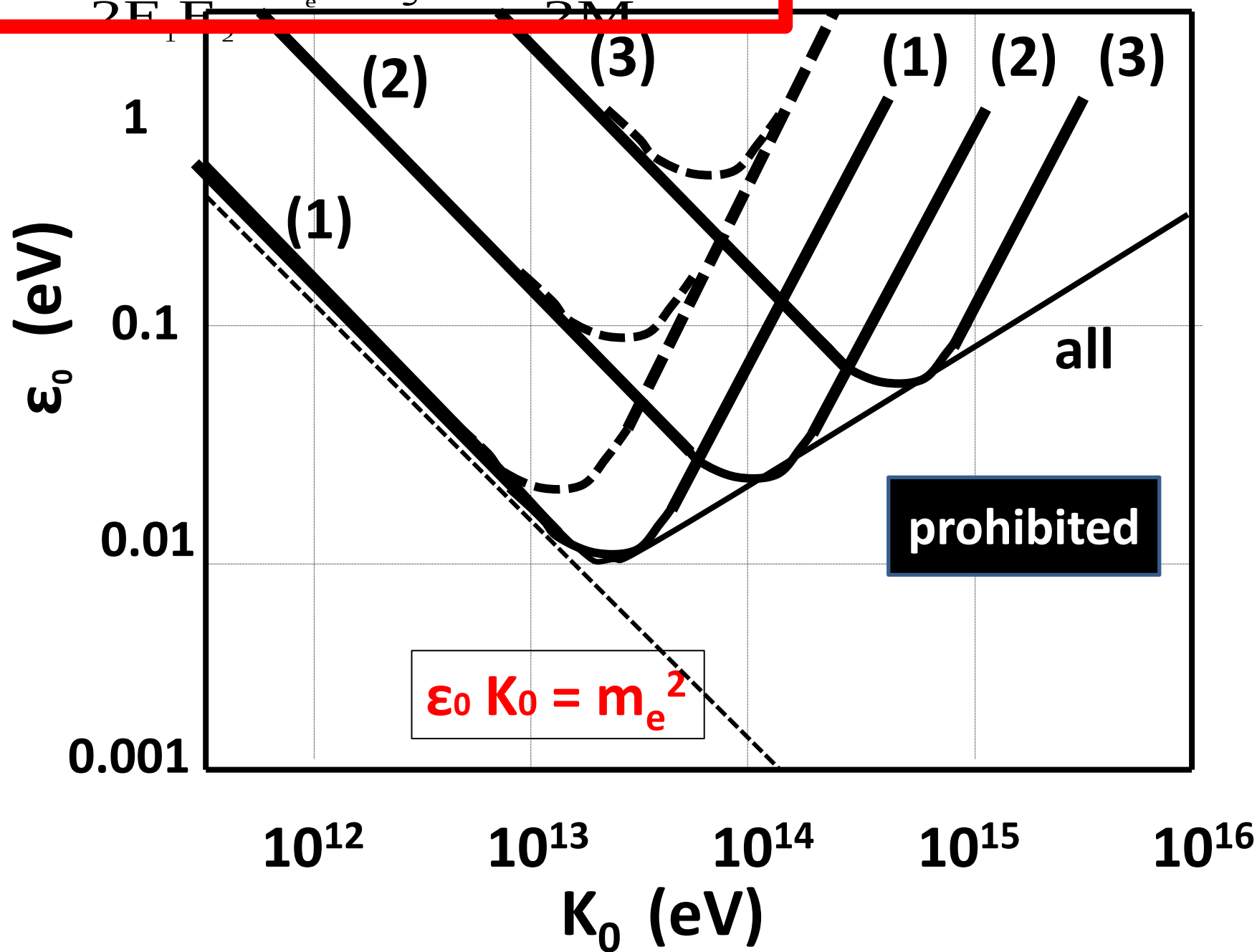
$$= p_1 + p_2 - p_1 \theta_1^2 / 2 - p_2 \theta_2^2 / 2$$

$$< p_1 + p_2$$

$$< E_1 + E_2 - Km^2 / (2E_1 E_2) \\ + \xi (E_1^2 + E_2^2) / (2M)$$

$$2\varepsilon > \frac{K_0}{2E_1 E_2} m_e^2 + \xi \frac{K_0^2 - E_1^2 - E_2^2}{2M}$$

$$2\varepsilon > \frac{K_0}{2E_1 E_2} m_e^2 + \xi \frac{K_0^2 - E_1^2 - E_2^2}{2M^2}$$



$$4\varepsilon > \frac{1}{K_0 a(1-a)} m_e^2 + \xi \frac{K_0^2 \cdot 2a(1-a)}{M} \quad a = \frac{E_1}{K_0}$$

$$1-a = \frac{E_2}{K_0} = \frac{K_0 - E_1}{K_0}$$

左边 > 右边第1項

threshold

左边 > 右边第2項

prohibition /suppression
of large K_0

右边第1項 $\approx$ 右边第2項

characteristic energy
“asymmetric parameter “a

characteristic /critical energies

$$\varepsilon_c = \left(\frac{m_e^4}{M}\right)^{1/3} \approx 10^{-2} \text{ eV}$$

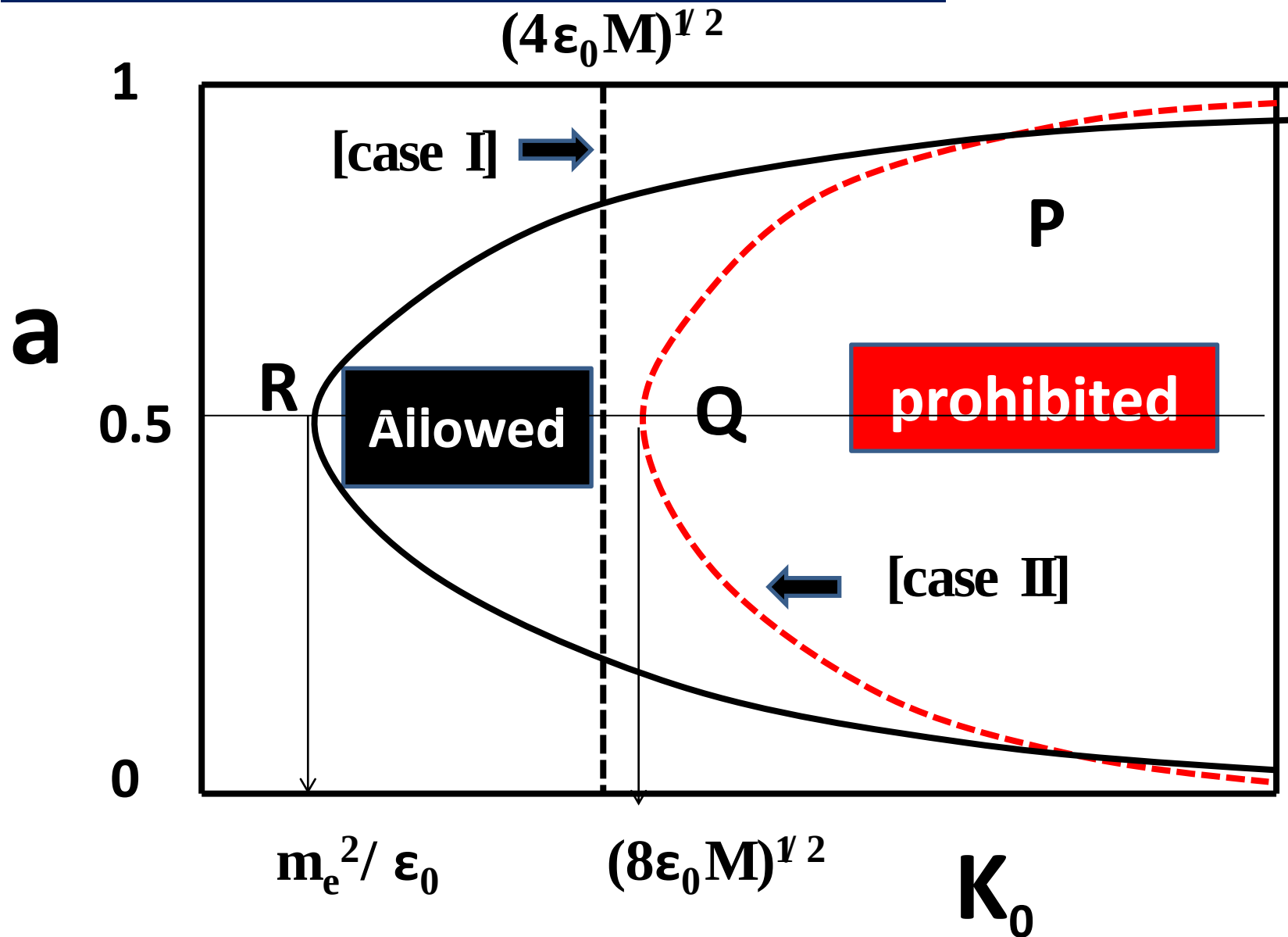
Infra Red

$$K_c = (m_e^2 M)^{1/3} \approx 10^{13} \text{ eV}$$

10-100 TeV

$$K_* = (\varepsilon M)^{1/2} \approx \frac{\varepsilon}{1 \text{ eV}} \cdot 10^{14} \text{ eV}$$

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^+ + e^-$$



Inverse Compton scattering

$$e + \varepsilon (\text{EBL}) \rightarrow e + \gamma$$

momentum : $\vec{p}_0 - \vec{\varepsilon} = \vec{p} + \vec{k}$

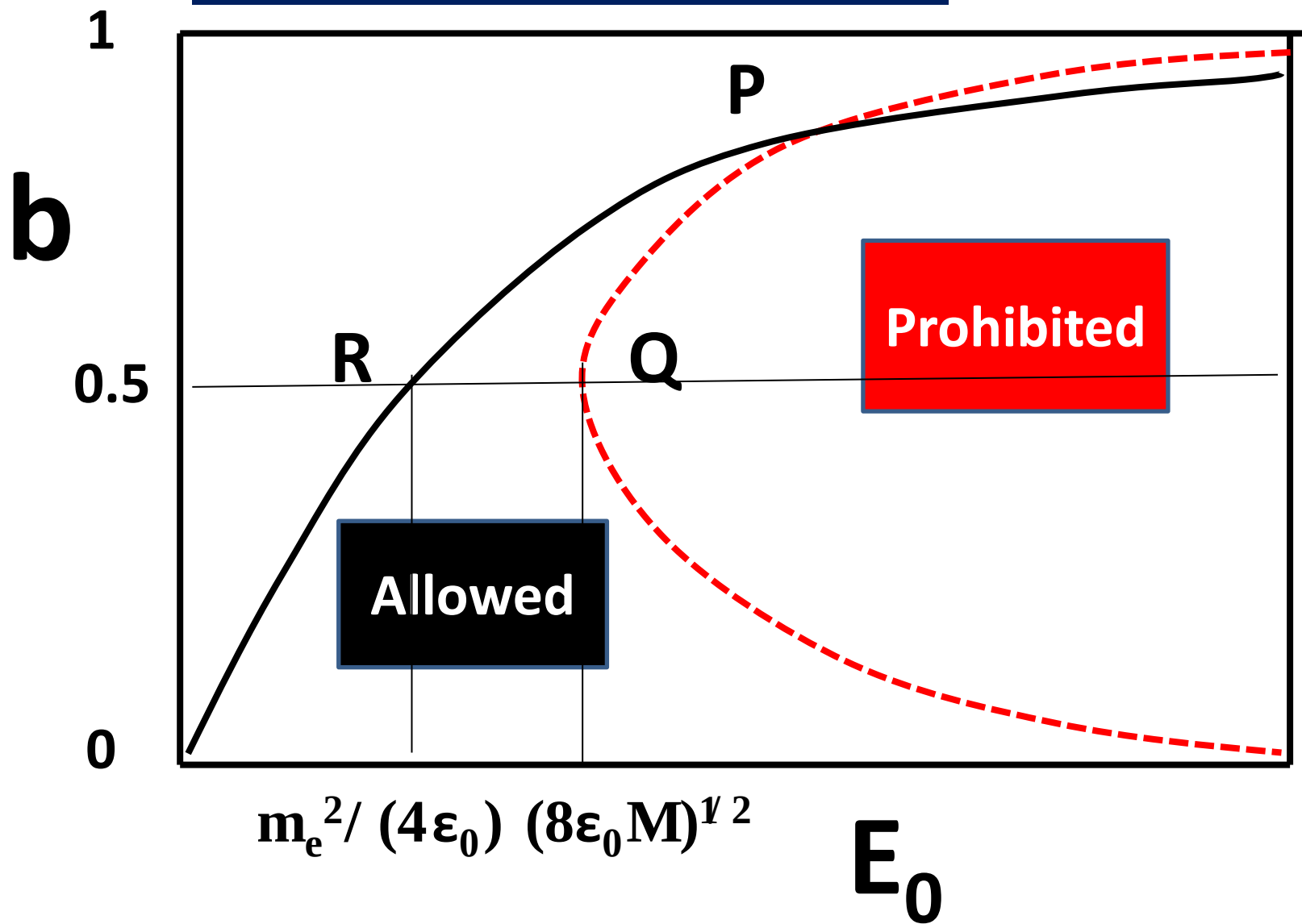
Energy : $E_0 + \varepsilon = E + K$

$$2\varepsilon > \frac{K}{2E_0 E} m_e^2 + \xi \frac{E_0^2 - E^2 - K^2}{2M}$$

$$2\varepsilon > \frac{b}{2E_0(1-b)} m_e^2 + \xi \frac{E_0^2 \cdot b(1-b)}{M}$$

$$b = K/E_0$$

$$e + \varepsilon(\text{EBL}) \rightarrow e + \gamma$$



IC/synchrotron radiation

$$e + \varepsilon (\text{EBL}) \rightarrow e + \gamma$$

$$2\varepsilon > \frac{K}{2E_0 E} m_e^2 + \xi \frac{E_0^2 - E^2 - K^2}{2M}$$

$$2\varepsilon > \frac{b}{2E_0(1-b)} m_e^2 + \xi \frac{E_0^2 \cdot b(1-b)}{M}$$

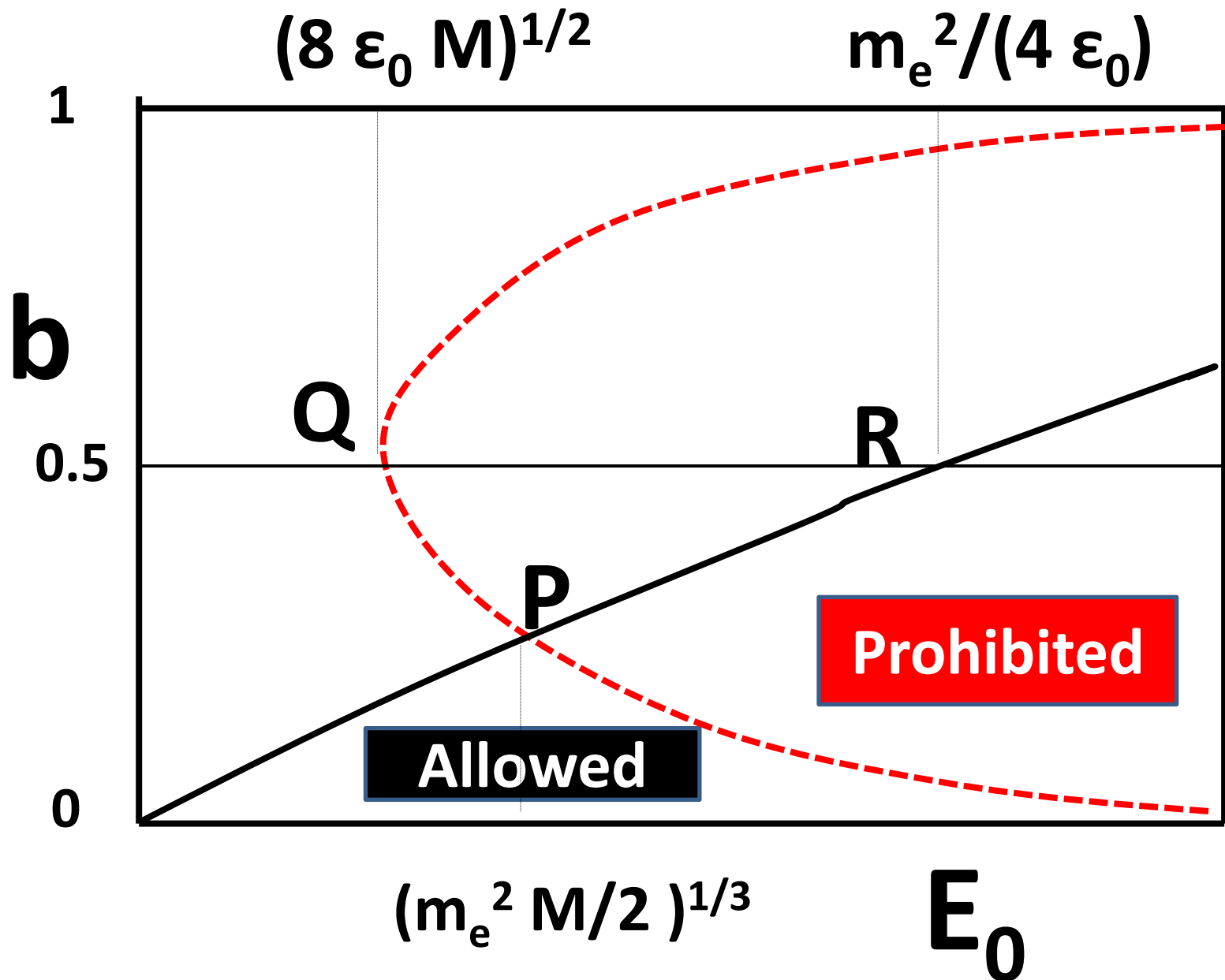
$$b = K/E_0$$

$$K < \frac{4\varepsilon E_0}{m_e^2 + 4\varepsilon E_0} E_0 \approx \frac{4\varepsilon E_0^2}{m_e^2}$$

$$K < 4\varepsilon \left(\frac{E_0}{m_e} \right)^2 \cdot \frac{1}{1 + \frac{2E_0^3}{m_e^2 M}}$$

$e + \varepsilon \text{ (EBL)} \rightarrow e + \gamma$

synchrotron radiation



Effects on interaction/process

- Prohibition of reaction

$$(\varepsilon M)^{1/2}$$

- Suppression

$$(m_e^2 M)^{1/3}$$

- **Asymmetric energy partition
for final particles**

Asymmetric
energy partition

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^- + e^+$$

$$4K_0\varepsilon > Am_e^2 + \xi \frac{K_0^2}{M}$$

$$a = E_1/K_0$$

$$A = 1/(a(1-a))$$

Left > 1 st or 2 nd term of right side

$$\frac{A}{4\varepsilon} m_e^2 < K_0 < \sqrt{4\varepsilon M}$$

$$\frac{A}{4\varepsilon} m_e^2 < K_0 < \sqrt{2\varepsilon AM}$$

$$\frac{K_0^2}{2\varepsilon M} < A < \frac{2\varepsilon^3 M}{m_e^4}$$

1 st $\nlessgtr$ 2 nd term of right side

$$A > \frac{K_0^3}{m_e^2 M} = 0.4 \cdot \left(\frac{K_0}{10^{13}}\right)^3$$

$$A > \sqrt{\frac{2K_0^3}{m_e^2 M}} = 0.9 \cdot \left(\frac{K_0}{10^{13}}\right)^{3/2}$$

Extensive Air Showers

e^-e^+ pair creation
bremsstrahlung



From Rene Ong's talk

$$\gamma + \gamma_b \text{ (EBL)} \rightarrow e^+ + e^-$$

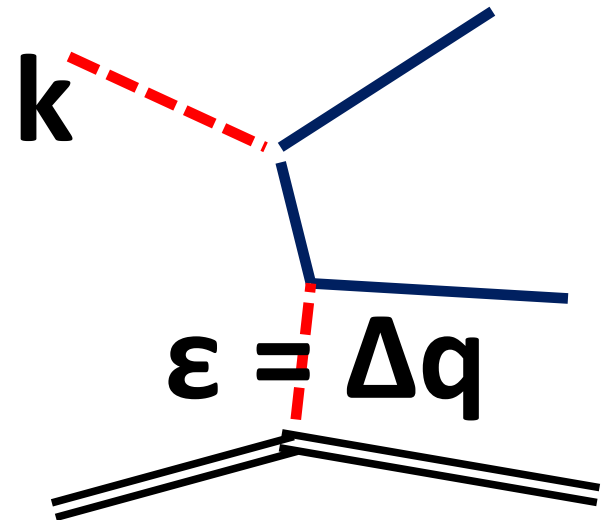
momentum : $\vec{k} - \vec{\varepsilon} = \vec{p}_1 + \vec{p}_2$

$$\gamma + A \rightarrow e^+ + e^- + A$$

momentum : $\vec{k} = \vec{p}_1 + \vec{p}_2 + \vec{\Delta q}$

$$\varepsilon \rightarrow \Delta q$$

$$\Delta q > \frac{K_0}{2E_1 E_2} m_e^2 + \xi \frac{K_0^2 - E_1^2 - E_2^2}{2M}$$



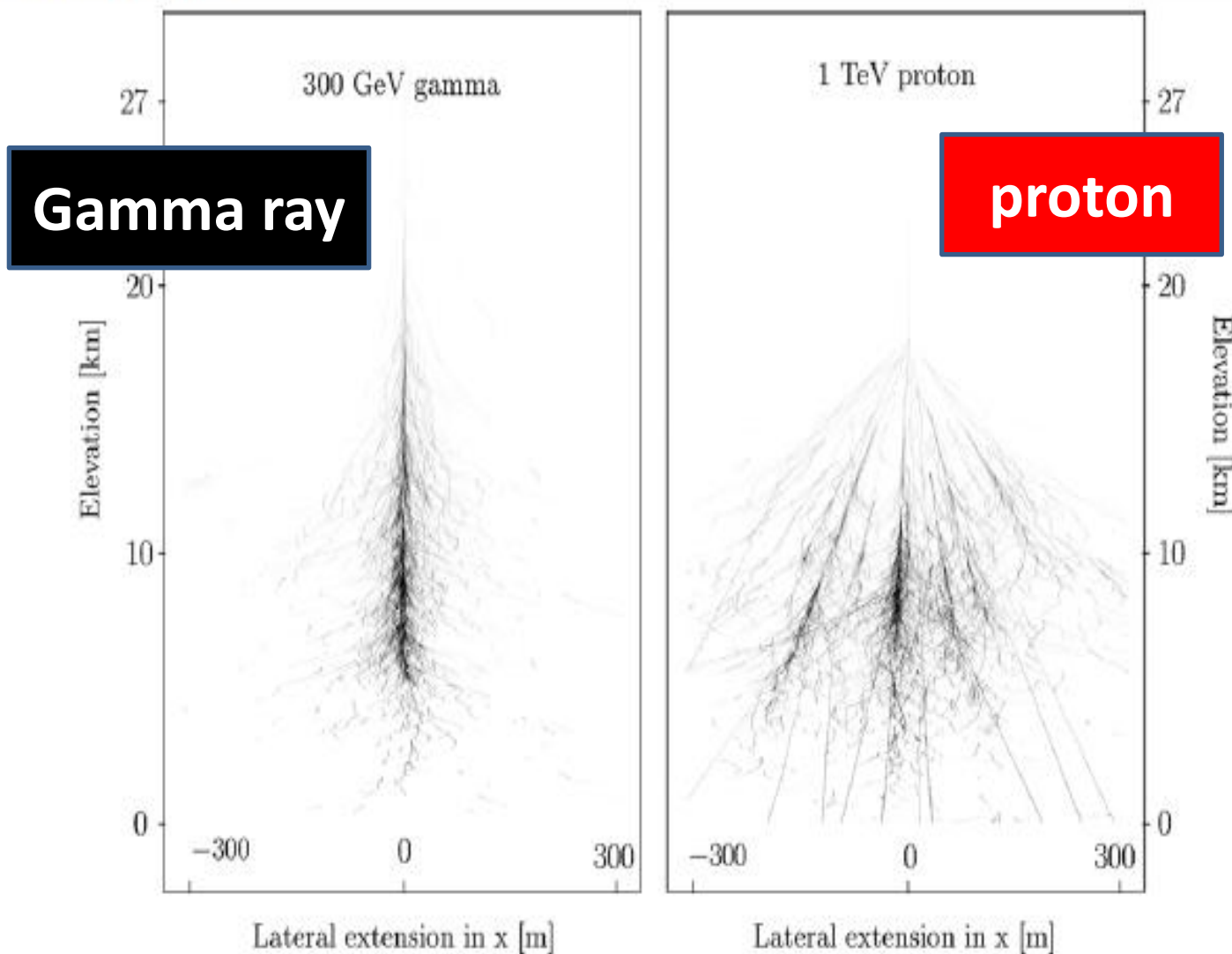
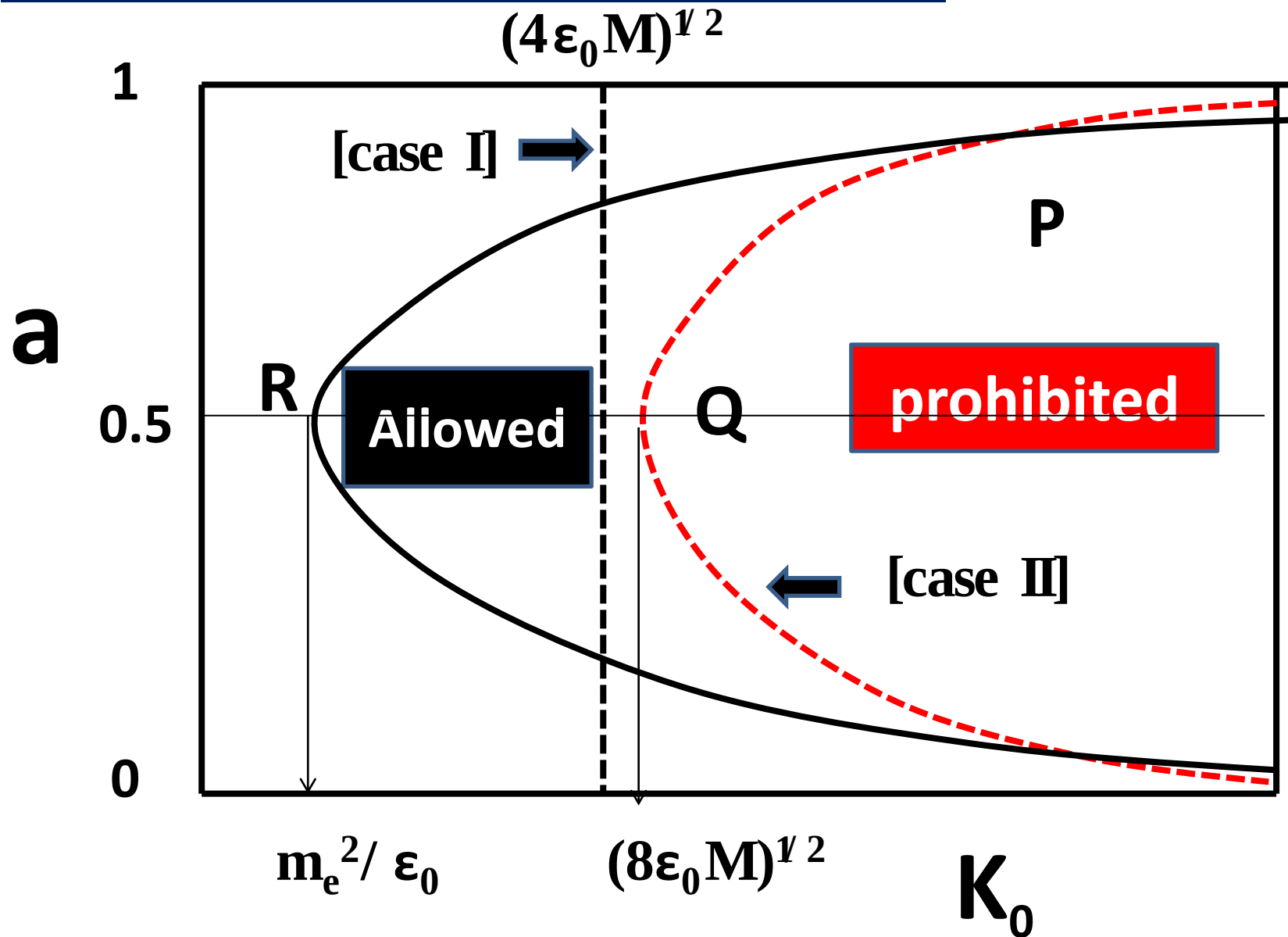
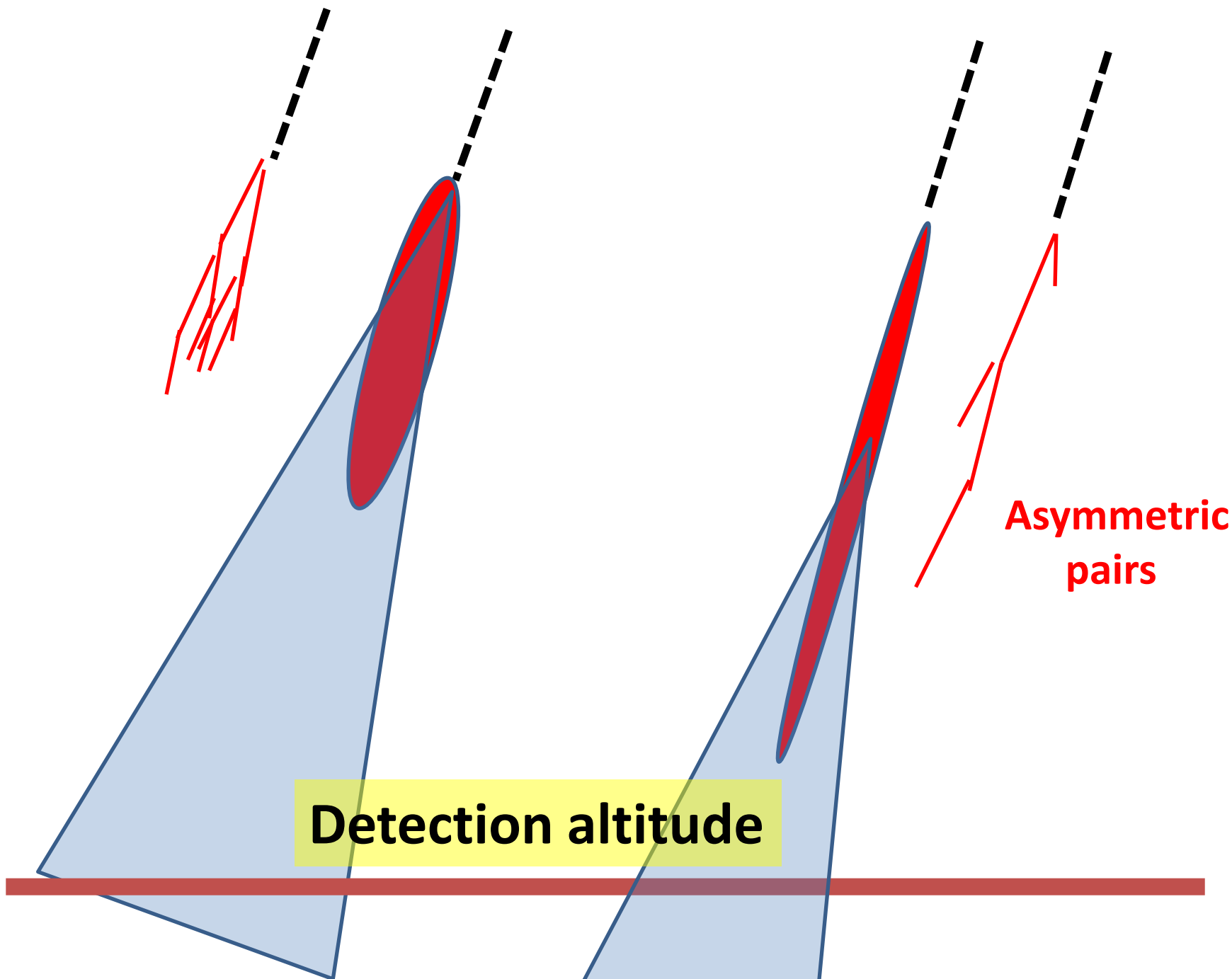


Figure 7. Comparison of a pure electromagnetic shower (from a 300 GeV γ ray) and a hadronic shower (initiated by a 1 TeV proton). The plot shows the projection of secondary particle trajectories onto an (x, z) plane (courtesy of Stefan Funk).

$$\gamma + \varepsilon (\text{EBL}) \rightarrow e^+ + e^-$$





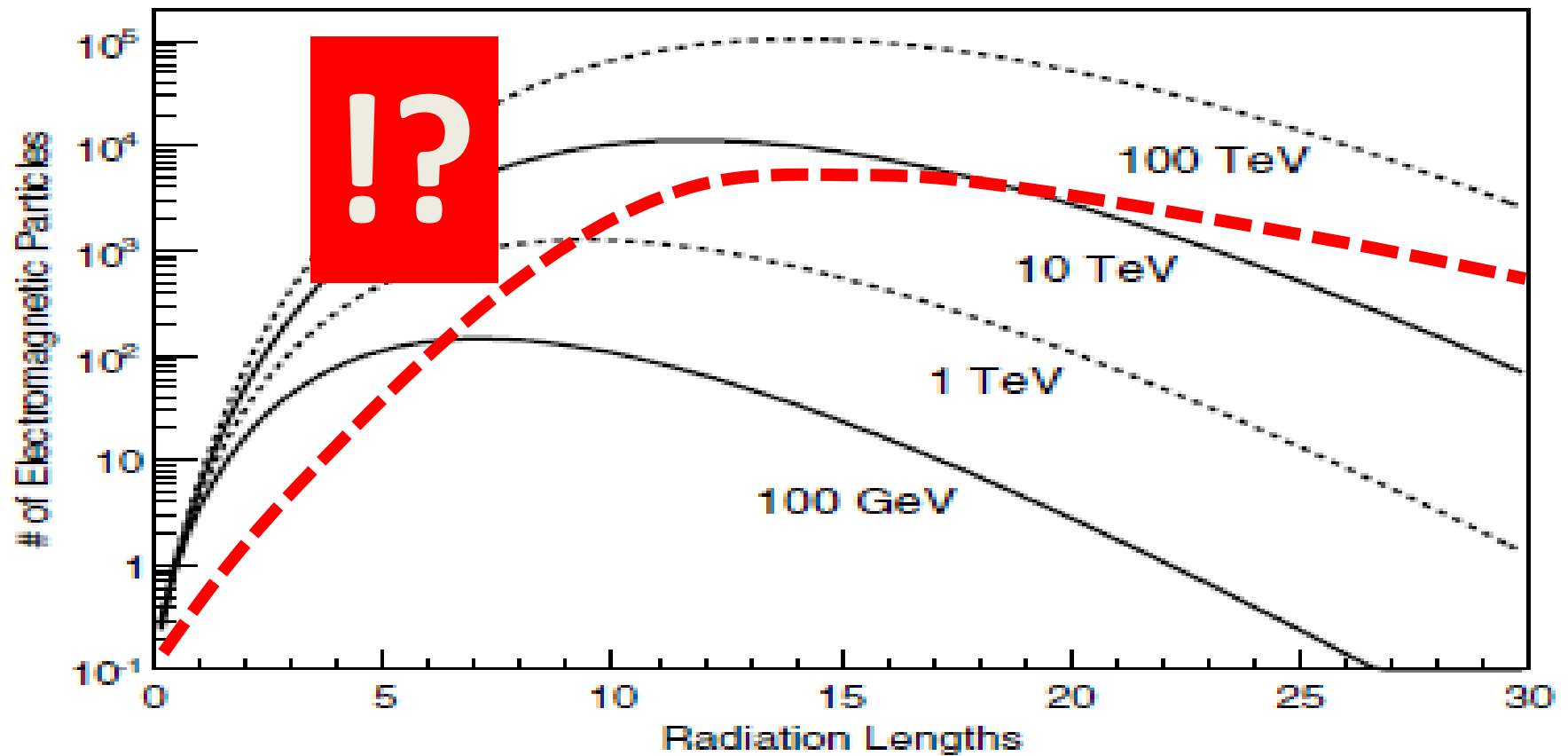


Figure 4. The longitudinal development of an extensive air shower as given by approximation B for several different primary gamma ray energies. The x -axis is the atmospheric depth expressed as the number of radiation lengths. The y -axis gives the number of electromagnetic particles in the air shower. Sea level is ~ 28 radiation lengths of atmosphere, 2600 m above sea level is ~ 20 radiation lengths, 4300 m above sea level is ~ 16.5 radiation lengths and 5200 m above sea level is ~ 14.7 radiation lengths.

$$\gamma + A \rightarrow e^+ + e^- + A$$

The case of
all particles are
relativistic

momentum : $\vec{k} = \vec{p}_1 + \vec{p}_2 + \vec{p}_A$

$$2K_0 m_A > \frac{K_0(K_0 - E_A)}{E_1 E_2} m_e^2 + \frac{K_0}{E_A} m_A^2 + \xi \frac{K_0^2 - E_1^2 - E_2^2 - E_A^2}{2M}$$

$$E_1 \rightarrow K_0$$

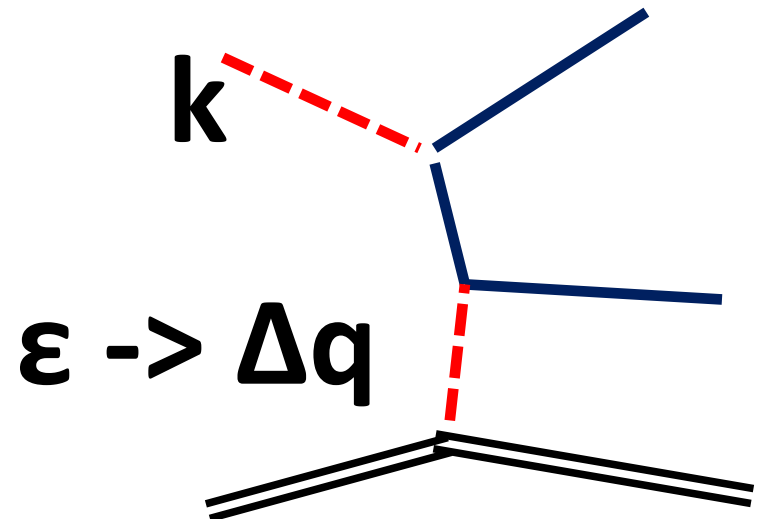
or

$$E_2 \rightarrow K_0$$

or

$$E_A \rightarrow K_0$$

favored



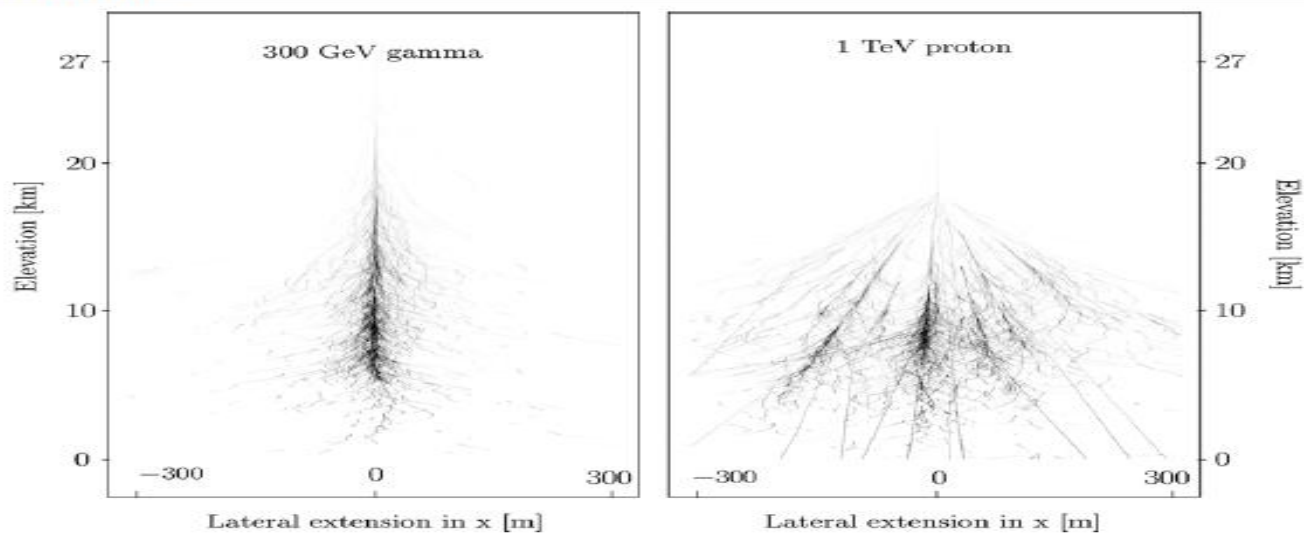
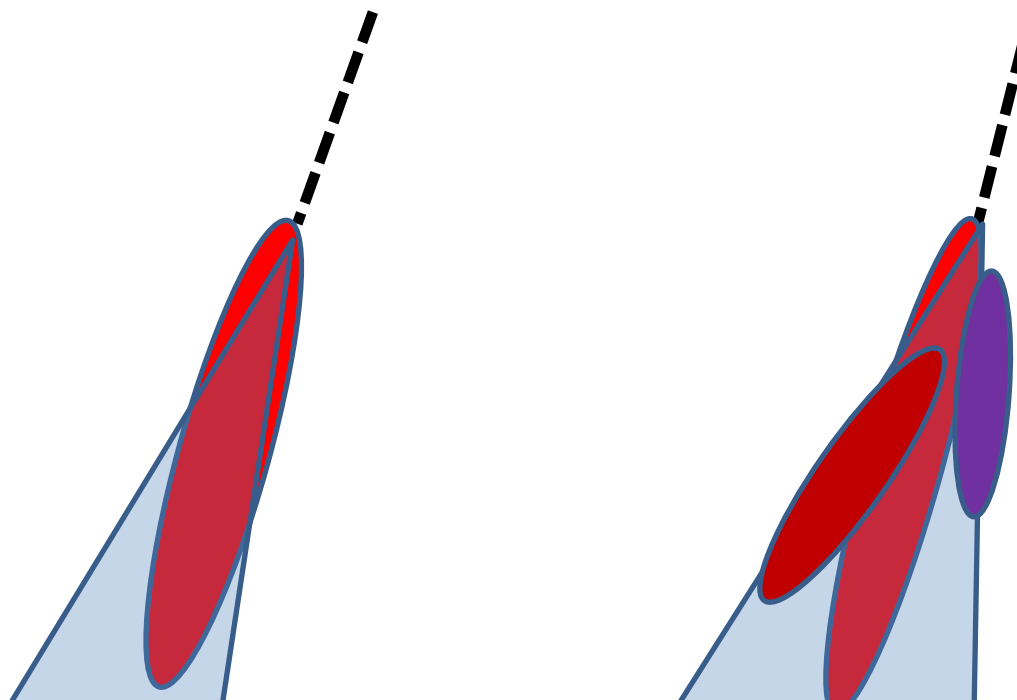


Figure 7. Comparison of a pure electromagnetic shower (from a 300 GeV γ ray) and a hadronic shower (initiated by a 1 TeV proton). The plot shows the projection of secondary particle trajectories onto an (x, z) plane (courtesy of Stefan Funk).

Gamma-ray initiated Extensive Air Shower ?

- **Slow development of EAS**

**Penetrating deeper to the bottom
of atmosphere**

- **High altitudes $\leftrightarrow$ sea level ?**

**At least, it is necessary
to compare the results at different altitudes**

- **Proton-like shower.....**

muon content ?

width, concentration

Cygnus X-3

Results 1983

Crimea

Experiment Details

Kiel Experiment:
claim 4.4σ signal.

28 counters, each 1 m^2
Energy: 1-10 PeV

4.8 hr periodicity

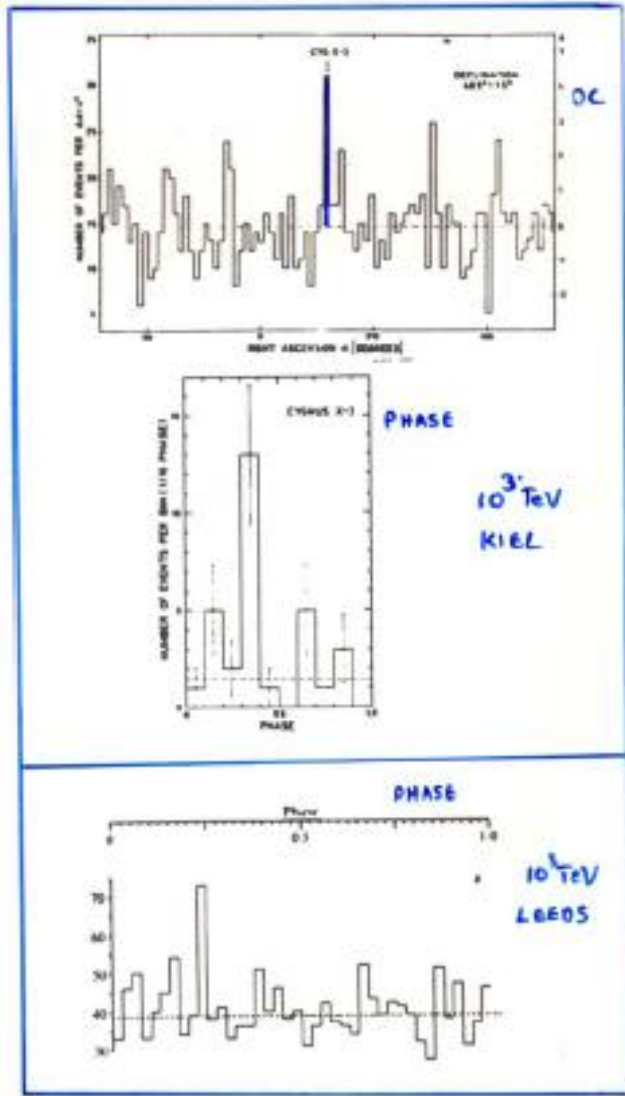
**Not
muon poor !?**

**Time variable
Recently detected by Fermi**

Haverah Park
 $\sim 4\sigma$ effect.

4 large water
Cherenkov detectors.
Energy $> 1 \text{ PeV}$

**Adding some words
onto a slide from Rene Ong's**



summary

- Extragalactic gamma ray of $10^{14} - 10^{15}$ eV

We badly need

clear evidence for quantum gravity effect

gamma rays from nearby galaxies $\leftrightarrow$ CR physics

- Suppression of IC, synchrotron radiation
for $E_0 > 10^{13} - 10^{14}$ eV

$\rightarrow$ SSC model lepton/hadron model.. ..

- Detection method ?

Are we driving a right vehicle

along the paved road / right road ?

toward the destination we are heading for ?

- Many other effects
- Prospect for gamma ray astronomy/CR physics
will be dramatically changed